Multiple positive solutions for some semilinear elliptic equations

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We prove existence of multiple positive solutions for the problem

$$Lu = f(u)$$
 in $D, u = 0$ on ∂D ,

where L is a linear differential operator in general form and f is a concave-convex nonlinearity. Several different applications are considered. Proofs involve a combination of the method of sub and supersolutions and index theory.